

TSI VIDE

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Steps for TSI Videos

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- ① $|-7| - |-3|$ video 1
- ② $|-2 - (-8)|$ video 2
- ③ If $a=3$, $b=-5$ find $\frac{a-b}{b}$ video 33
- ④ If $x=5$, $y=3$ find $3x+5y$ video 34
- ⑤ $(3-2) - (2-3)$ video 73
- ⑥ $-2 - (-8)$ video 78
- ⑦ $-(4-6) - (2-6)$ video 79
- ⑧ $(-\frac{1}{2})^2$ video 100
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Simplify

3.

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20 $13a - 15b - a + 2b$ video 63

21 $(2a - 7b + 1) - (a - 7b + 2)$ video 64

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27 $-4(9r + 7) + 6(3r + 5)$ video 70

28 $7x + 6 + 3x - x + 4$ video 71

29 $(12x - x) - (3y - 15y)$ video 77

Solve

(30) $x - 10 = 5x - 10$ video 15

(31) $3 + N = 2N$ find $8N$ video 16

(4)

(32) $3x = 7 - 5x$ video 17

(33) $\frac{x+2}{3} = \frac{2x-1}{4}$ video 49

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(35) $6 - x = 2(x - 6)$ video 75

(36) $2x + 1 = 4x + 9$ video 84

(37) $2(2x + 4) = 12$ video 85

(38) $2x + 1 = 4x + 1$ video 86

(39) $2x + 2 = 2x + 8$ video 87

(40) $6 - x = -2(6 - x)$ video 88

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(44) $1.95x + 10 = 1.90x + 30$ video 151

(45) $2(2x + 4) = 2x + 20$ video 153

Solve

(46) $1 + 2x \leq 3x - 5$ video 18 (5)

(47) $3a > a + 8$ video 19

(48) $\frac{x}{4} - \frac{3x}{8} > 0$ video 20

(49) $0 < x - 3 < 5$ video 21

(50) $-2x + 1 < 21$ video 126

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(52) $-4 < 2x + 6 < 4$ video 207

Simplify

(53) $(1+xy)(1-xy)$ video 22

(54) $(x-8y)(x-8y)$ video 23

(55) $(4z+7)(2z+5)$ video 24

(56) $(2x+1)(1-ax)$ video 25

(57) $(3x-2)(4x+c)=12x^2+x-6$ find c video 91

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(60) $(4x-3y)^2$ video 102

(61) $(2-xy)^2$ video 103

(62) $x(x-2)-3x(x+2)$ video 104

(63) $x(x-5)-4x(x-5)$ video 120

(64) $(x-2)x+(2-x)3x$ video 121

(65) $(x+2)(x^2-3x+5)$ video 157

Factor

- (66) $a(x-y) + (x-y)$ factor video 26
- (67) $b^2 - 6b - 16$ factor video 27 (7)
- (68) $25 - \frac{x^2}{4}$ factor video 28
- (69) $3x^3 - 9x^2 + 6x$ factor video 29
- (70) $b^2 - bc - 2c^2$ factor video 30
- (71) $x^3 - x^2 - 2x$ factor video 31
- (72) $\frac{a^2}{4} - \frac{1}{9}$ factor video 32
- (73) $x^3 + 6x^2 + 8x$ factor video 105
- (74) $2x^3 + 2x^2 - 8x - 8$ factor video 106
- (75) $25x^2 - 64y^2$ factor video 109
- (76) $x^2 - 10x + 16$ factor video 112
- (77) $x^2 - 4x - 12$ factor video 113
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- (81) $2x^2 - 32y^2$ factor video 127
- (82) $3x^2 - 27y^2$ factor video 138

Solve

8.

83. $x^2 - x = 2$ solve by factoring Video 108

84. $2x^2 + 10x - 48 = 0$ solve by factoring video 115

85. $x^2 - 6x - 40 = 0$ solve by factoring video 116

86. $x^2 + 3 = 4x$ solve by factoring video 123

87. $x^2 - 6x + 18 = 0$ solve by
using the Quadratic formula
video 180

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Simplify

(88) $\frac{x^2 - 5x + 6}{2x^2 + 4x - 16}$ simplify video 118

(89) $\frac{3x - 6}{x^2 - 4}$ simplify video 119

9.

(90) $\frac{-24x^2y^2 + 12xy^2 + 28xy}{4xy}$ simplify video 124

(91) $\frac{-48x^2}{36x}$ simplify video 136

(92) $\frac{20x^3y^4}{30x^5y^2}$ simplify video 137

(93) $\frac{x}{4x - 16} \div \frac{x^2 - 2x}{x - 4}$ simplify video 139

(94) $\left(\frac{x^3}{18y}\right)\left(\frac{6y}{4x^2}\right)$ simplify video 143

(95) $(2x^2 - 5x - 7) \div (x - 1)$ use synthetic division video 154

(96) $\frac{m^2 - 16}{m^2 + 3m - 28} \div \frac{m^2 - 3m - 28}{m - 4}$ simplify video 155

(97) $\left(\frac{4a^3b^9c^4}{-8a^5b^{-2}c^{-2}}\right)^4$ simplify video 197

Solve

(98) $x + 2y = 7$ Solve video 50
 $x = 5y$

(99) $y = 2x + 4$ Solve video 51
 $y = x - 5$

(100) $x - y = 0$ Solve video 52
 $x + y = 2$

(101) $x - y = 0$ Solve video 53
 $2x - y = 1$

(102) $x + y = 6$ Solve video 54
 $x = 2y$

(103) $2x - y = 6$ Solve video 135
 $2x + y = 6$

(104) $2x - 3y = 2$ Solve video 194
 $4x - 6y = 1$

(105) $N + D = 100$ Solve video 202
 $.05N + .10D = 9.50$

Solve

(106) $|x+2|=4$ Solve video 55

(107) $|x+2|<6$ Solve video 56

(108) $|x+2|>8$ Solve video 57

(109) $|x-2|=4$ Solve video 58

(110) $|r-2|=5$ Solve video 162

(111) $|x+9|<15$ Solve video 163

(112) $|x+6|>16$ Solve video 164

(113) $y=2x-2$ Graph video 165

(114) $y=2x+4$ Graph video 210

(115) $f(x)=x^2-4$ Graph video 188

(116) $f(x)=x^2$ and $g(x)=(x-1)^2+4$
graph video 198

(117) $\frac{ax-b}{a-1} \div b$ find x video 9

(118) $y=mb^2$ find b video 141

(119) $2^{x+1}=16$ find x video 200

11

120. Find the equation of the line with slope $m=3$ thru point $(-3,6)$. Video 167

121. Find the equation of the line thru the two points $(10,800)$ and $(12,900)$ video 208

122. Find the distance between the two points $(5,-2)$ and $(2,2)$. Video 173

123. Find the midpoint between the two points $(4,-8)$ and $(-10,2)$. Video 183

124. $f(x) = -x^2 + 4x + 5$ Find the y-intercept
Video 186

125. $f(x) = -x^2 + 4x + 5$ Find the x-intercept
Video 187

(126) $f(x) = 4x^2 - 8x - 9$ and $g(x) = -2x^2 - 3x + 5$
 find $(f-g)(x)$ video 159 (12)

(127) $f(x) = 2x^2 + 3x + 4$, find $f(x-1)$ video 160

(128) $f(x) = x^2 + 6$ find $f(a+h)$ video 178

(129) $f(x) = x^2 + 8x - 6$, find $\frac{f(x+h) - f(x)}{h}$ video 179

(130) $f(x) = 2x + 3$ and $g(x) = 5x + 8$
 find $(f \circ g)(x)$ video 181

(131) $f(x) = 2x + 3$ and $g(x) = x^2 + 6x - 5$
 find $(g \circ f)(x)$ video 182

(132) $f(x) = -1(x-2)^2 + 9$ find the vertex video 184

(133) $f(x) = -x^2 + 4x + 5$ find the vertex video 185
 (use vertex formula)

(134) $f(x) = -250x^2 + 2500x + 50,000$ find the
 maximum value (use vertex formula) video 199

(135) $f(x) = 4x^2 - 3$ and $g(x) = 5x + 4$

find $(f \circ g)(x)$ video 203

(14)

(136) $f(x) = 3x - 6$ and $g(x) = x^2 - 4$

find $(\frac{f}{g})(x)$ video 204

(137) $\sqrt{180}$ simplify video 168

(138) $\sqrt{169x^6y^9z^9}$ simplify video 169

(139) $\sqrt{3x^3} \sqrt{6x^2}$ simplify video 170

(140) $\frac{2}{8 - \sqrt{3}}$ rationalize the denominator video 171

(141) $\sqrt{7-x} = x-1$ solve video 172

(142) $\sqrt[3]{-27a^{11}b^{13}}$ simplify video 174

(15)

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Step by Step solutions

$$\textcircled{1} \quad |-7| - |-3| =$$

$$(7) - (3) =$$

$$7 - 3 =$$

$$\textcircled{4} =$$

16

$$\textcircled{2} \quad |-2 - (-8)| =$$

$$|-2 + 8| =$$

$$|6| =$$

$$(6) =$$

$$\textcircled{6} =$$

$$\textcircled{3} \quad \text{If } a = 3, \quad b = -5 \quad \text{find } \frac{a-b}{b}$$

$$\frac{a-b}{b} =$$

$$\frac{(3) - (-5)}{(-5)} =$$

$$\frac{3 + 5}{-5} =$$

$$\frac{8}{-5} =$$

$$\textcircled{-\frac{8}{5} =}$$

(4) If $x=5$, $y=3$ find $3x+5y$

$$3x+5y=$$

$$3(5)+5(3)=$$

$$15+15=$$

$$30=$$

17.

(5) $(3-2)-(2-3)=$

$$(1)-(-1)=$$

$$1+1=$$

$$2=$$

(6) $-2-(-8)=$

$$-2+8=$$

$$6=$$

(7) $-(4-6)-(2-6)=$

$$-(-2)-(-4)=$$

$$2+4=$$

$$6=$$

$$8. \left(-\frac{1}{2}\right)^2 =$$

$$\left(-\frac{1}{2}\right)\left(-\frac{1}{2}\right) =$$

$$\frac{1}{4} =$$

$$18.$$

$$9. (8-2) - (2-8) =$$

$$(6) - (-6) =$$

$$6 + 6 =$$

$$12 =$$

$$10. \text{ If } x = -2, y = -6 \text{ find } x^2 - y^2$$

$$x^2 - y^2 =$$

$$(-2)^2 - (-6)^2 =$$

$$(-2)(-2) - (-6)(-6) =$$

$$(4) - (36) =$$

$$4 - 36 =$$

$$-32 =$$

11. If $y = -2x^2 - 5x + 2$ Eval if $x = -4$

$$y = -2x^2 - 5x + 2$$

$$y = -2(-4)^2 - 5(-4) + 2$$

$$y = -2(-4)(-4) - 5(-4) + 2$$

$$y = -2(16) - 5(-4) + 2$$

$$y = -32 + 20 + 2$$

$$y = -12 + 2$$

$$y = -10$$

19

12. If $y = -2(x+4)^2 - 8$ Eval if $x = -6$

$$y = -2(x+4)^2 - 8$$

$$y = -2((-6)+4)^2 - 8$$

$$y = -2(-6+4)^2 - 8$$

$$y = -2(-2)^2 - 8$$

$$y = -2(-2)(-2) - 8$$

$$y = -2(4) - 8$$

$$y = -8 - 8$$

$$y = -16$$

(13) If $y = 2(x-2) - 10$ Eval if $x = -6$

$$y = 2(x-2) - 10$$

$$y = 2((-6)-2) - 10$$

$$y = 2(-6-2) - 10$$

$$y = 2(-8) - 10$$

$$y = -16 - 10$$

$$y = -26$$

26

(14) If $f(x) = -2x^2 - 4x + 6$ find $f(-5)$

$$f(x) = -2x^2 - 4x + 6$$

$$f(-5) = -2(-5)^2 - 4(-5) + 6$$

$$f(-5) = -2(-5)(-5) - 4(-5) + 6$$

$$f(-5) = -2(25) - 4(-5) + 6$$

$$f(-5) = -50 + 20 + 6$$

$$f(-5) = -30 + 6$$

$$f(-5) = -24$$

(15.) If $h(x) = 3x^2 - 7x - 4$ find $h(-5)$

$$h(x) = 3x^2 - 7x - 4$$

$$h(-5) = 3(-5)^2 - 7(-5) - 4$$

$$h(-5) = 3(-5)(-5) - 7(-5) - 4$$

$$h(-5) = 3(25) - 7(-5) - 4$$

$$h(-5) = 75 + 35 - 4$$

$$h(-5) = 110 - 4$$

$$h(-5) = 106$$

(16.) If $f(x) = |5x - 4|$ find $f(-3)$

$$f(x) = |5x - 4|$$

$$f(-3) = |5(-3) - 4|$$

$$f(-3) = |-15 - 4|$$

$$f(-3) = |-19|$$

$$f(-3) = (19)$$

$$f(-3) = 19$$

17. If $4x+2y=8$ is $(x,y)=(1,2)$ a solution?
x y

$$4x+2y=8 \quad ?$$

$$4(1)+2(2)=8 \quad ?$$

$$4+4=8 \quad ?$$

$$8=8 \quad \checkmark$$

yes

22

18. $8\sqrt{5}+3\sqrt{5}-\sqrt{5} =$ simplify

$$8\sqrt{5}+3\sqrt{5}-1\sqrt{5} =$$

$$11\sqrt{5}-1\sqrt{5} =$$

$$10\sqrt{5} =$$

19. $15x^2y + 4xy^2 - 2xy^2 + 3x^2y =$
 $15x^2y + 4xy^2 - 2xy^2 + 3x^2y =$

$$18x^2y + 2xy^2 =$$

20. $13a - 15b - a + 2b =$
 $13a - 15b - 1a + 2b =$
 $12a - 13b =$

23

21. $(2a - 7b + 1) - (a - 7b + 2) =$
 $(2a - 7b + 1) - (1a - 7b + 2) =$
 $2a - 7b + 1 - 1a + 7b - 2 =$
 $1a - 1 =$
 $a - 1 =$

22. $(x^2 - 3x + 2) - (3x^2 - 5x - 1) =$
 $1x^2 - 3x + 2 - 3x^2 + 5x + 1 =$
 $-2x^2 + 2x + 3 =$

23. $7x^2 - (8x^2 - x) =$
 $7x^2 - 8x^2 + x =$
 $-1x^2 + x =$
 $-x^2 + x$

(24.)

$$2x + 3x + y =$$

$$5x + y =$$

(24.)

(25.)

$$(x-3) - 3(x+2) =$$

$$x-3 - 3x-6 =$$

$$1x-3-3x-6 =$$

$$-2x-9 =$$

(26.)

$$(x^2-5) - (x^2+6) =$$

$$x^2-5-x^2-6 =$$

$$1x^2-5-1x^2-6 =$$

$$-11 =$$

(27.)

$$-4(9r+7) + 6(3r+5) =$$

$$-36r - 28 + 18r + 30 =$$

$$-18r + 2 =$$

(28.)

$$7x+6+3x-x+4 =$$

$$7x+6+3x-(x+4) =$$

$$9x+10 =$$

$$\begin{aligned}
 (29) \quad & (12x - x) - (3y - 15y) = \\
 & (12x - 1x) - (3y - 15y) = \\
 & (11x) - (-12y) = \\
 & 11x + 12y =
 \end{aligned}$$

251

$$\begin{aligned}
 (30) \quad & x - 10 = 5x - 10 \\
 & x - 10 + 10 = 5x - 10 + 10 \\
 & x = 5x \\
 & x - 5x = 5x - 5x \\
 & 1x - 5x = 0 \\
 & -4x = 0 \\
 & \frac{-4x}{-4} = \frac{0}{-4} \\
 & x = 0
 \end{aligned}$$

$$\begin{aligned}
 (31) \quad & 3 + N = 2N \quad \text{find } 8N \\
 & 3 + \cancel{N} - \cancel{N} = 2N - N \\
 & 3 = 2N - 1N \\
 & 3 = 1N \\
 & 3 = N
 \end{aligned}$$

→ subs
 $8N =$
 $8(3) =$
 24

$$\textcircled{32} \quad 3x = 7 - 5x$$

$$3x + 5x = 7 - \cancel{5x} + \cancel{5x}$$

$$8x = 7$$

$$\frac{\cancel{8x}}{\cancel{8}} = \frac{7}{8}$$

$$x = \frac{7}{8}$$

26

$$\textcircled{33} \quad \frac{x+2}{3} = \frac{2x-1}{4}$$

$$4(\widehat{x+2}) = 3(\widehat{2x-1}) \quad \text{cross mult}$$

$$4x + 8 = 6x - 3$$

$$4x + \cancel{8} - \cancel{8} = 6x - 3 - 8$$

$$4x = 6x - 11$$

$$4x - 6x = 6x - 11 - 6x$$

$$-2x = -11$$

$$\frac{-2x}{-2} = \frac{-11}{-2}$$

$$x = \frac{11}{2}$$

34

$$2x - 3(x - 4) = -5$$

$$2x - 3x + 12 = -5$$

$$-1x + 12 = -5$$

$$-1x + \cancel{12} - \cancel{12} = -5 - 12$$

$$-1x = -17$$

$$\frac{-1x}{-1} = \frac{-17}{-1}$$

$$x = 17$$

27

35.

$$6 - x = 2(x - 6)$$

$$6 - x = 2x - 12$$

$$\cancel{6} - x - \cancel{6} = 2x - 12 - 6$$

$$-x = 2x - 18$$

$$-x - 2x = \cancel{2x} - 18 - \cancel{2x}$$

$$-1x - 2x = -18$$

$$-3x = -18$$

$$\frac{-3x}{-3} = \frac{-18}{-3}$$

$$x = 6$$

36

$$2x + 1 = 4x + 9$$

$$2x + \cancel{1} - \cancel{1} = 4x + 9 - 1$$

$$2x = 4x + 8$$

$$2x - 4x = 4x + 8 - 4x$$

$$-2x = 8$$

$$\frac{-2x}{-2} = \frac{8}{-2}$$

$$x = -4$$

28

37

$$2(2x + 4) = 12$$

$$4x + 8 = 12$$

$$4x + \cancel{8} - \cancel{8} = 12 - 8$$

$$4x = 4$$

$$\frac{4x}{4} = \frac{4}{4}$$

$$x = 1$$

38

$$2x + 1 = 4x + 1$$

$$2x + \cancel{1} - \cancel{1} = 4x + \cancel{1} - \cancel{1}$$

$$2x = 4x$$

$$2x - 4x = 4x - 4x$$

$$-2x = 0$$

$$\frac{-2x}{-2} = \frac{0}{-2}$$

$$x = 0$$

$$\begin{aligned}
 (39) \quad 2x+2 &= 2x+8 \\
 2x+\cancel{2}-\cancel{2} &= 2x+8-2 \\
 2x &= 2x+6 \\
 2x-2x &= 2x+6-2x
 \end{aligned}$$

(29)

$$0 \neq 6$$

No solution



$$\begin{aligned}
 (40) \quad 6-x &= -2(6-x) \\
 6-x &= -12+2x \\
 \cancel{6}-x-\cancel{6} &= -12+2x-\cancel{6} \\
 -x &= 2x-18 \\
 -x-2x &= 2x-18-2x \\
 -1x-2x &= -18 \\
 -3x &= -18 \\
 \frac{-3x}{-3} &= \frac{-18}{-3}
 \end{aligned}$$

$$x=6$$

$$\begin{aligned}
 (41) \quad \text{If } 4x-8 &= 2x \quad \text{find } 12x \rightarrow \frac{2x}{2} = \frac{8}{2} \\
 4x-\cancel{8}+\cancel{8} &= 2x+8 \\
 4x &= 2x+8 \\
 4x-2x &= 2x+8-2x \\
 2x &= 8
 \end{aligned}$$

$$x=4$$

$$\begin{aligned}
 \text{find } 12x &= \\
 12(4) &=
 \end{aligned}$$

$$24 =$$

$$(42) \quad \frac{4x}{3} = 6 - \frac{x}{4}$$

$$\text{LCD} = 12$$

30

$$\frac{4x}{3} = \frac{6}{1} - \frac{x}{4}$$

$$\frac{4x}{3}(12) = \frac{6}{1}(12) - \frac{x}{4}(12)$$

$$4x(4) = 6(12) - x(3)$$

$$16x = 72 - 3x$$

$$16x + 3x = 72 - 3x + 3x$$

$$19x = 72$$

$$\frac{19x}{19} = \frac{72}{19}$$

$$x = \frac{72}{19}$$

$$(43) \quad \frac{x}{2} - \frac{1}{4} = 3 + \frac{5x}{6}$$

$$\text{LCD} = 12$$

$$\frac{x}{2} - \frac{1}{4} = \frac{3}{1} + \frac{5x}{6}$$

$$-4x = 39$$

$$\frac{x}{2}(12) - \frac{1}{4}(12) = \frac{3}{1}(12) + \frac{5x}{6}(12)$$

$$\frac{-4x}{-4} = \frac{39}{-4}$$

$$x(6) - 1(3) = 3(12) + 5x(2)$$

$$x = -\frac{39}{4}$$

$$6x - 3 = 36 + 10x$$

$$6x - 3 + 3 = 36 + 10x + 3$$

$$6x = 10x + 39$$

$$6x - 10x = 10x + 39 - 10x$$

44.

$$1.95x + 10 = 1.90x + 30$$

$$1.95x + \cancel{10} - \cancel{10} = 1.90x + 30 - 10$$

$$1.95x = 1.90x + 20$$

$$1.95x - 1.90x = 1.90x + 20 - 1.90x$$

$$.05x = 20$$

$$\frac{.05x}{.05} = \frac{20}{.05}$$

$$x = 400$$

31.

45.

$$2(2x + 4) = 2x + 20$$

$$4x + 8 = 2x + 20$$

$$4x + \cancel{8} - \cancel{8} = 2x + 20 - 8$$

$$4x = 2x + 12$$

$$4x - 2x = 2x + 12 - 2x$$

$$2x = 12$$

$$\frac{2x}{2} = \frac{12}{2}$$

$$x = 6$$

46. $1 + 2x \leq 3x - 5$

32.

~~$1 + 2x - 1 \leq 3x - 5 - 1$~~

$2x \leq 3x - 6$

$2x - 3x \leq 3x - 6 - 3x$

$-1x \leq -6$

$\frac{-1x}{-1} \geq \frac{-6}{-1}$ Turn all signs

$x \geq 6$



$[6, \infty)$

47. $3a > a + 8$

$3a - a > a + 8 - a$

$3a - 1a > 8$

$2a > 8$

$\frac{2a}{2} > \frac{8}{2}$

$a > 4$

48. $\frac{x}{4} - \frac{3x}{8} > 0$

$L(0) = 8$

$\frac{-1x}{-1} < \frac{0}{-1}$

$\frac{x}{4}(8) - \frac{3x}{8}(8) > 0(8)$

$x(2) - 3x(1) > 0$

$2x - 3x > 0$

$-1x > 0$

$x < 0$

(49) $0 < x - 3 < 5$

$$0 + 3 < x - 3 + 3 < 5 + 3$$

$$3 < x < 8$$

33.

(50) $-2x + 1 < 21$

$$-2x + 1 - 1 < 21 - 1$$

$$-2x < 20$$

$$\frac{-2x}{-2} > \frac{20}{-2}$$

$$x > -10$$

(51) $18 - 3x \geq -12$

$$18 - 3x - 18 \geq -12 - 18$$

$$-3x \geq -30$$

$$\frac{-3x}{-3} \leq \frac{-30}{-3}$$

$$x \leq 10$$

(52) $-4 < 2x + 6 < 4$

$$-4 - 6 < 2x + 6 - 6 < 4 - 6$$

$$-10 < 2x < -2$$

$$\frac{-10}{2} < \frac{2x}{2} < \frac{-2}{2}$$

$$-5 < x < -1$$

$$(53) \quad (1+xy)(1-xy) =$$

$$1 - \cancel{1xy} + \cancel{1xy} - x^2y^2 =$$

$$1 - x^2y^2 =$$

39.

$$(54) \quad (x-8y)(x-8y) =$$

$$x^2 - 8xy - 8xy + 64y^2 =$$

$$x^2 - 16xy + 64y^2 =$$

$$(55) \quad (4z+7)(2z+5) =$$

$$8z^2 + 20z + 14z + 35 =$$

$$8z^2 + 34z + 35 =$$

$$(56) \quad (2x+1)(1-ax) =$$

$$2x - 2ax^2 + 1 - 1ax =$$

$$2x - 2ax^2 + 1 - ax =$$

57 $(3x-2)(4x+c) = 12x^2 + x - 6$ find c

$$-2c = -6$$

$$\frac{-2c}{-2} = \frac{-6}{-2}$$

$$c = 3$$

351

58 $A^2 + N + 2B^2 = (A+B)(A+2B)$ find N

$$= A^2 + 2AB + AB + 2B^2$$

$$= A^2 + 2AB + 1AB + 2B^2$$

$$= A^2 + 3AB + 2B^2$$

$$N = 3AB$$

59 $\left(\frac{6x}{2}\right)^2 =$

$$(3x)^2 =$$

$$(3x)(3x) =$$

$$9x^2 =$$

60. $(4x-3y)^2 =$

$(4x-3y)(4x-3y) =$

$16x^2 - 12xy - 12xy + 9y^2 =$

$16x^2 - 24xy + 9y^2 =$

36

61. $(2-xy)^2 =$

$(2-xy)(2-xy) =$

$4 - 2xy - 2xy + x^2y^2 =$

$4 - 4xy + x^2y^2 =$

62. $x(x-2) - 3x(x+2) =$

$x^2 - 2x - 3x^2 - 6x =$

$1x^2 - 2x - 3x^2 - 6x =$

$-2x^2 - 8x =$

63. $x(x-5) - 4x(x-5) =$

$x^2 - 5x - 4x^2 + 20x =$

$1x^2 - 5x - 4x^2 + 20x =$

$-3x^2 + 15x =$

64. $(x-2)x + (2-x)3x =$
 $x^2 - 2x + 6x - 3x^2 =$
 $1x^2 - 2x + 6x - 3x^2 =$
 $-2x^2 + 4x =$

37.

65. $(x+2)(x^2-3x+5) =$
 $x^3 - 3x^2 + 5x + 2x^2 - 6x + 10 =$
 $x^3 - 1x^2 - 1x + 10 =$
 $x^3 - x^2 - x + 10 =$

66. $a(x-y) + (x-y) = \text{factor}$
 $a(x-y) + 1(x-y) =$
 $(x-y)(a+1) =$

67. $b^2 - 6b - 16 = \text{factor}$
 $(b+2)(b-8) =$

16.1 possible
 8.2
 4.4

68) $25 - \frac{x^2}{4} =$ factor

$$(5)^2 - \left(\frac{x}{2}\right)^2 =$$

$$\left(5 + \frac{x}{2}\right)\left(5 - \frac{x}{2}\right) =$$

$a^2 - b^2 = (a+b)(a-b)$
formula

38.

69) $3x^3 - 9x^2 + 6x =$ factor

$$3x(x^2 - 3x + 2) =$$

$$3x(x-1)(x-2) =$$

2.1

70) $b^2 - bc - 2c^2 =$ factor

$$(b+c)(b-2c) =$$

2.1

71) $x^3 - x^2 - 2x =$ factor

$$x(x^2 - x - 2) =$$

$$x(x+1)(x-2) =$$

$a^2 - b^2 = (a+b)(a-b)$
formula

72) $\frac{a^2}{4} - \frac{1}{9} =$ factor

$$\left(\frac{a}{2}\right)^2 - \left(\frac{1}{3}\right)^2 =$$

$$\left(\frac{a}{2} + \frac{1}{3}\right)\left(\frac{a}{2} - \frac{1}{3}\right) =$$

73 $X^3 + 6X^2 + 8X =$ factor

$$X(X^2 + 6X + 8) =$$

$$X(X+2)(X+4) =$$

8.1

2.4

Possible

39.

74 $2X^3 + 2X^2 - 8X - 8 =$ factor (Group)

$$(2X^3 + 2X^2) + (-8X - 8) =$$

$$2X^2(X+1) + 8(-X-1) =$$

$$2X^2(X+1) - 8(X+1) =$$

$$(X+1)(2X^2 - 8) =$$

$$(X+1)(2)(X^2 - 4) =$$

$$(X+1)(2)((X)^2 - (2)^2) =$$

$$(X+1)(2)(X+2)(X-2) =$$

$$2(X+1)(X+2)(X-2) =$$

$$a^2 - b^2 = (a+b)(a-b)$$

75 $25x^2 - 64y^2 =$ factor

$$(5x)^2 - (8y)^2 =$$

$$(5x+8y)(5x-8y) =$$

76 $X^2 - 10X + 16 =$ factor

$(X - 2)(X - 8) =$

16.1
2.8
4.4

40

77 $X^2 - 4X - 12 =$ factor

$(X + 2)(X - 6) =$

12.1
6.2
3.4

78 $X^2 + 6X - 16 =$ factor

$(X - 2)(X + 8) =$

16.1
2.8
4.4

79 $2X^2 + 4X - 16 =$ factor

$2(X^2 + 2X - 8) =$

$2(X - 2)(X + 4) =$

16.1
2.8
4.4

80 $8X^2Y^2 - 4X^2Y - 10XY^2 =$ factor

$2XY(4XY - 2X - 5Y) =$

81. $2x^2 - 32y^2 =$ factor

$$a^2 - b^2 = (a+b)(a-b)$$

formula

41

$$2(x^2 - 16y^2) =$$

$$2((x)^2 - (4y)^2) =$$

$$2(x+4y)(x-4y) =$$

82. $3x^2 - 27y^2 =$ factor

$$a^2 - b^2 = (a+b)(a-b)$$

formula

$$3(x^2 - 9y^2) =$$

$$3((x)^2 - (3y)^2) =$$

$$3(x+3y)(x-3y) =$$

83. $x^2 - x = 2$ solve

2.1

$$x^2 - x - 2 = 2 - 2$$

$$x^2 - x - 2 = 0$$

$$(x+1)(x-2) = 0$$

but $x+1=0$ OR $x-2=0$

$x+1=0-1$ OR $x-2+2=0+2$

$$x = -1$$

$$x = 2$$

84. $2x^2 + 10x - 48 = 0$ Solve

$$2(x^2 + 5x - 24) = 0$$

$$2(x - 3)(x + 8) = 0$$

24.1

12.2

6.4

3.8

42

Possible

Let $2 \neq 0$ OR $x - 3 = 0$ OR $x + 8 = 0$

$x - 3 + 3 = 0 + 3$ OR $x + 8 - 8 = 0 - 8$

$x = 3$

OR $x = -8$

85. $x^2 - 6x - 40 = 0$ Solve

$$(x + 4)(x - 10) = 0$$

40.1

20.2

10.4

5.8

Possible

Let $x + 4 = 0$ OR $x - 10 = 0$

$x + 4 - 4 = 0 - 4$ OR $x - 10 + 10 = 0 + 10$

$x = -4$

OR $x = 10$

Possible

3.1

86. $x^2 + 3 = 4x$

$$x^2 + 3 - 4x = 4x - 4x$$

$$x^2 + 3 - 4x = 0$$

$$x^2 - 4x + 3 = 0$$

$$(x - 1)(x - 3) = 0$$

Let

$x - 1 = 0$

OR

$x - 3 = 0$

$x - 1 + 1 = 0 + 1$

OR

$x - 3 + 3 = 0 + 3$

$x = 1$

OR

$x = 3$

(87) $x^2 - 6x + 18 = 0$ Solve use the Quadratic formula (43)

$$a=1, b=-6, c=18$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(1)(18)}}{2(1)}$$

$$x = \frac{6 \pm \sqrt{36 - 72}}{2}$$

$$x = \frac{6 \pm \sqrt{-36}}{2}$$

$$x = \frac{6 \pm 6i}{2}$$

$$x = 3 \pm 3i$$

$$x = 3 + 3i$$

OR

$$x = 3 - 3i$$

formula
 $\sqrt{-1} = i$

88. $\frac{x^2 - 5x + 6}{2x^2 + 4x - 16} =$ Simplify

44

$$\frac{x^2 - 5x + 6}{2(x^2 + 2x - 8)} =$$

$$\frac{(x-2)(x-3)}{2(x-2)(x+4)} =$$

$$\frac{x-3}{2(x+4)} =$$

89. $\frac{3x-6}{x^2-4} =$

$$\frac{3(x-2)}{(x)^2 - (2)^2} =$$

$$\frac{3(x-2)}{(x+2)(x-2)} =$$

$$\frac{3}{x+2} =$$

$$(90) \quad \frac{-24x^2y^2 + 12xy^2 + 28xy}{4xy} = \text{simplify} \quad (45)$$

$$\frac{-24x^2y^2}{4xy} + \frac{12xy^2}{4xy} + \frac{28xy}{4xy} =$$

$$-6xy + 3y + 7 =$$

$$(91) \quad \frac{-48x^2}{36x} = \text{simplify}$$

$$\frac{-4(\cancel{12})x^2}{3(\cancel{12})x^1} =$$

$$\frac{-4x}{3} =$$

$$(92) \quad \frac{20x^3y^4}{30x^5y^2} = \text{simplify}$$

$$\frac{2(\cancel{10})x^3y^4}{3(\cancel{10})x^5y^2} =$$

$$\frac{2y^2}{3x^2} =$$

93. $\frac{x}{4x-16} \div \frac{x^2-2x}{x-4} = \text{Simplify}$

46

$$\frac{x}{4x-16} \cdot \frac{x-4}{x^2-2x} =$$

$$\frac{\cancel{x}}{4(\cancel{x}-4)} \cdot \frac{(\cancel{x}-4)}{x(x-2)} =$$

$$\frac{1}{4(x-2)} =$$

94. $\left(\frac{x^3}{18y}\right)\left(\frac{6y}{4x^2}\right) = \text{Simplify}$ Primes 2, 3, 5, 7

$$\frac{\cancel{x} \cdot \cancel{x} \cdot \check{x}}{\cancel{2} \cdot \check{3} \cdot \check{3} \cdot \cancel{y}} \cdot \frac{\cancel{2} \cdot \cancel{3} \cdot \cancel{y}}{\cancel{2} \cdot \check{2} \cdot \cancel{x} \cdot \cancel{x}} =$$

$$\frac{x}{12} =$$

$$\begin{array}{r} 2 \overline{)18} \\ 3 \overline{)9} \\ 3 \overline{)3} \\ 1 \end{array} \quad \begin{array}{r} 2 \overline{)6} \\ 3 \overline{)3} \\ 1 \end{array} \quad \begin{array}{r} 2 \overline{)4} \\ 2 \overline{)2} \\ 1 \end{array}$$

$$18 = 2 \cdot 3 \cdot 3$$

$$6 = 2 \cdot 3$$

$$4 = 2 \cdot 2$$

95. $(2x^2 - 5x - 7) \div (x-1)$ use synthetic division

$$\begin{array}{r|rrrr} & 2x^2 - 5x - 7 & = & & \\ & x-1 & & & \\ \hline 1 & 2 & -5 & -7 & \\ & & 2 & -3 & \\ \hline & 2 & -3 & -10 & \text{rem} \end{array}$$

$$2x - 3 + \frac{-10}{x-1}$$

OR

$$2x - 3 - \frac{10}{x-1}$$

96. $\frac{m^2 - 16}{m^2 + 3m - 28} \div \frac{m^2 - 3m - 28}{m-4} =$

$$\frac{m^2 - 16}{m^2 + 3m - 28} \cdot \frac{m-4}{m^2 - 3m - 28} =$$

$$\frac{(m+4)(m-4)}{(m-4)(m+7)} \cdot \frac{(m-4)}{(m+4)(m-7)} =$$

$$\frac{m-4}{(m+7)(m-7)} =$$

97. $\left(\frac{4a^3 b^4 c^4}{-8a^5 b^{-2} c^{-2}} \right)^4 =$

48

$$\left(\frac{4a^3 c^4 b^2 c^2}{-8a^5 b^9} \right)^4 =$$

$$\left(\frac{4a^3 c^6 b^2}{-8a^5 b^9} \right)^4 =$$

$$\left(\frac{1c^6}{-2a^{5-3} b^{9-2}} \right)^4 =$$

$$\left(\frac{c^6}{-2a^2 b^7} \right)^4 =$$

$$\frac{c^{24}}{(-2)^4 a^8 b^{28}} =$$

$$\frac{c^{24}}{16 a^8 b^{28}} =$$

98

$$x + 2y = 7$$

$$x = 5y$$

Solve by subst

49

$$(5y) + 2y = 7$$

$$5y + 2y = 7$$

$$7y = 7$$

$$\frac{7y}{7} = \frac{7}{7}$$

$$y = 1$$

Subst

$$x = 5y$$

$$x = 5(1)$$

$$x = 5$$

$$(x, y) = (5, 1)$$

99

$$y = 2x + 4$$

$$y = x - 5$$

Solve Subst

$$(2x + 4) = x - 5$$

$$2x + 4 = x - 5$$

$$2x + 4 - 4 = x - 5 - 4$$

$$2x = x - 9$$

$$2x - x = x - 9 - x$$

$$1x = -9$$

$$x = -9$$

Subst

$$y = 2x + 4$$

$$y = 2(-9) + 4$$

$$y = -18 + 4$$

$$y = -14$$

$$(x, y) = (-9, -14)$$

100

$$\begin{aligned} x - y &= 0 \\ x + y &= 2 \end{aligned}$$

$$2x + 0 = 2$$

$$2x = 2$$

$$\frac{2x}{2} = \frac{2}{2}$$

$$x = 1$$

Solve

Subst

$$x - y = 0$$

$$(1) - y = 0$$

$$1 - y = 0$$

$$x - y + 1 = 0 - 1$$

$$-y = -1$$

$$\frac{-y}{-1} = \frac{-1}{-1}$$

$$y = 1$$

$$(x, y) = (1, 1)$$

50

101

$$\begin{aligned} x - y &= 0 \\ 2x - y &= 1 \end{aligned}$$

$$(x - y)(-1) = 0(-1)$$

$$(2x - y)(1) = 1(1)$$

$$-x + y = 0$$

$$2x - y = 1$$

$$x = 1$$

Solve

Subst

$$x - y = 0$$

$$(1) - y = 0$$

$$1 - y = 0$$

$$x - y + 1 = 0 - 1$$

$$-y = -1$$

$$\frac{-y}{-1} = \frac{-1}{-1}$$

$$y = 1$$

$$(x, y) = (1, 1)$$

102

$$x + y = 6$$

$$x = 2y$$

$$(2y) + y = 6$$

$$2y + y = 6$$

$$3y = 6$$

$$\frac{3y}{3} = \frac{6}{3}$$

$$y = 2$$

Subst

$$x = 2y$$

$$x = 2(2)$$

$$x = 4$$

51

$$(x, y) = (4, 2)$$

103

$$2x - y = 6$$

$$2x + y = 6$$

$$4x + 0 = 12$$

$$4x = 12$$

$$\frac{4x}{4} = \frac{12}{4}$$

$$x = 3$$

Subst

Subst

$$2x - y = 6$$

$$2(3) - y = 6$$

$$6 - y = 6$$

$$6 - y - 6 = 6 - 6$$

$$-y = 0$$

$$\frac{-y}{-1} = \frac{0}{-1}$$

$$y = 0$$

$$(x, y) = (3, 0)$$

$$\begin{array}{r} 104 \quad 2x - 3y = 2 \\ 4x - 6y = 1 \end{array}$$

57

$$\begin{array}{r} (2x - 3y = 2) (-6) \text{ mult} \\ (4x - 6y = 1) (3) \end{array}$$

$$-12x + 18y = -12$$

$$12x - 18y = 3$$

$$0 + 0 = -9$$

$$0 \neq -9$$

No Solution

$$\begin{array}{r} 105 \quad N + D = 100 \\ .05N + .10D = 9.50 \end{array}$$

$$(N + D)(-.10) = 100(-.10) \text{ mult}$$

$$(.05N + .10D)(1) = 9.50(1)$$

$$-.10N - .10D = -10.00$$

$$.05N + .10D = 9.50$$

$$-.05N = -.50$$

$$\frac{-.05N}{-.05} = \frac{-.50}{-.05}$$

$$N = 10$$

Subst

$$N + D = 100$$

$$10 + D = 100$$

$$10 + D - 10 = 100 - 10$$

$$D = 90$$

$$(N, D) = (10, 90)$$

106 $|x+2|=4$ solve

$|x|=a$
 $x=-a$ OR $x=a$

$x+2=-4$ OR $x+2=4$

$x+2-2=-4-2$ OR $x+2-2=4-2$

$x=-6$

OR

$x=2$

107 $|x+2|<6$ solve

$|x|<a$
 $-a<x<a$

$-6<x+2<6$

$-6-2<x+2-2<6-2$

$-8<x<4$

108 $|x+2|>8$ solve

$|x|>a$
 $x<-a$ OR $x>a$

$x+2<-8$ OR $x+2>8$

$x+2-2<-8-2$ OR $x+2-2>8-2$

$x<-10$

OR

$x>6$

109 $|x-2|=4$ solve

$|x|=a$
 $x=-a$ OR $x=a$

$x-2=-4$ OR $x-2=4$

$x-2+2=-4+2$ OR $x-2+2=4+2$

$x=-2$

OR

$x=6$

(110) $|r-2|=5$ solve

$|x|=a$
 $x=-a$ OR $x=a$

$r-2=-5$ OR $r-2=5$

$r-2+2=-5+2$ OR $r-2+2=5+2$

$r=-3$ OR $r=7$

(111) $|x+9|<15$ solve

$|x|<a$
 $-a<x<a$

$-15<x+9<15$

$-15-9<x+9-9<15-9$

$-24<x<6$

(112) $|x+6|>16$

$|x|>a$
 $x<-a$ OR $x>a$

$x+6<-16$ OR $x+6>16$

$x+6-6<-16-6$ OR $x+6-6>16-6$

$x<-22$ OR $x>10$

113 $y = 2x - 2$ graph

$$y = 2(0) - 2$$

$$y = 0 - 2$$

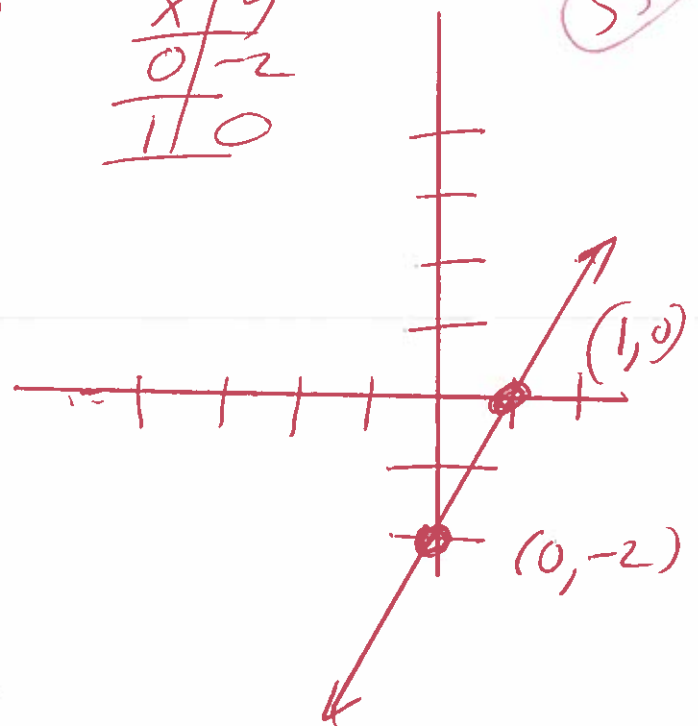
$$y = -2$$

$$y = 2(1) - 2$$

$$y = 2 - 2$$

$$y = 0$$

x	y
0	-2
1	0



114 $y = 2x + 4$ graph

$$y = 2(0) + 4$$

$$y = 0 + 4$$

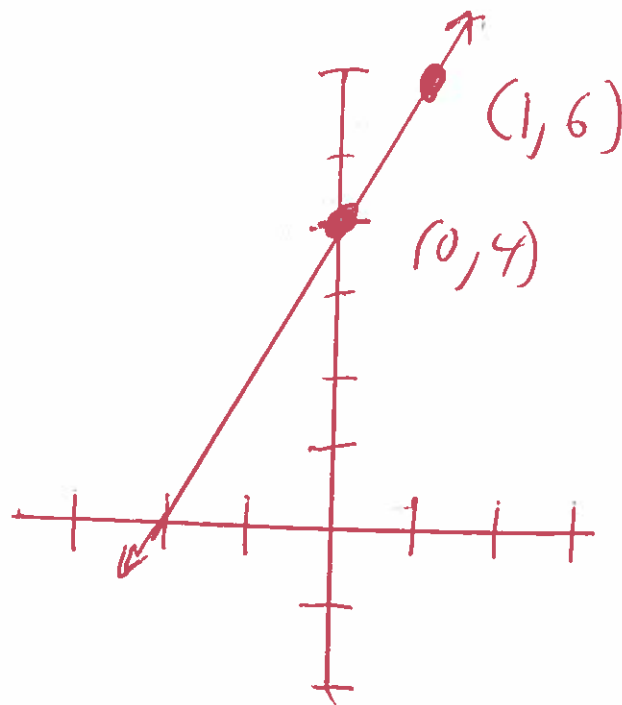
$$y = 4$$

$$y = 2(1) + 4$$

$$y = 2 + 4$$

$$y = 6$$

x	y
0	4
1	6



115 $f(x) = x^2 - 4$ graph

$$f(-1) = (-1)^2 - 4$$

$$f(-1) = (-1)(-1) - 4$$

$$f(-1) = 1 - 4$$

$$f(-1) = -3$$

x	y
-1	-3
0	-4
1	-3

(56)

$$f(0) = (0)^2 - 4$$

$$f(0) = (0)(0) - 4$$

$$f(0) = 0 - 4$$

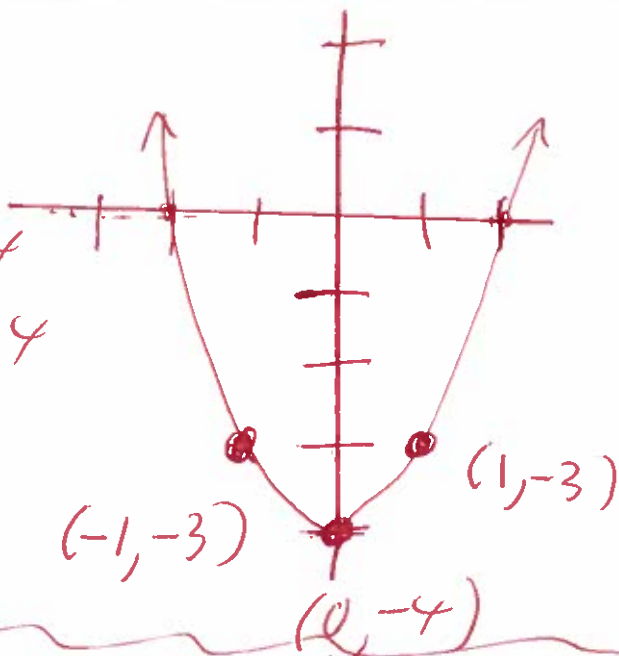
$$f(0) = -4$$

$$f(1) = (1)^2 - 4$$

$$f(1) = (1)(1) - 4$$

$$f(1) = 1 - 4$$

$$f(1) = -3$$



116 $f(x) = x^2$ and $g(x) = (x-1)^2 + 4$

$$f(-1) = (-1)^2$$

$$f(-1) = (-1)(-1)$$

$$f(-1) = 1$$

$$f(0) = (0)^2$$

$$f(0) = (0)(0)$$

$$f(0) = 0$$

$$f(1) = (1)^2$$

$$f(1) = (1)(1)$$

$$f(1) = 1$$

x	y
-1	1
0	0
1	1

$$g(x) = (x-1)^2 + 4$$

$$g(0) = (0-1)^2 + 4$$

$$g(0) = (-1)^2 + 4$$

$$g(0) = 1 + 4$$

$$g(0) = 5$$

$$g(1) = (1-1)^2 + 4$$

$$g(1) = (0)^2 + 4$$

$$g(1) = 0 + 4$$

$$g(1) = 4$$

$$g(2) = (2-1)^2 + 4$$

$$g(2) = (1)^2 + 4$$

$$g(2) = 1 + 4$$

$$g(2) = 5$$

x	y
0	5
1	4
2	5

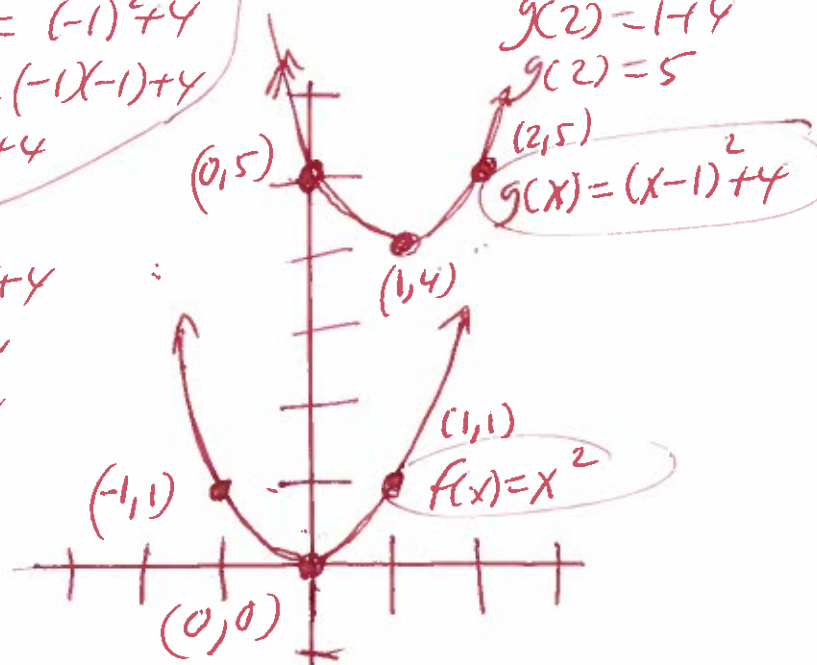
$$g(2) = (2-1)^2 + 4$$

$$g(2) = (1)^2 + 4$$

$$g(2) = (1)(1) + 4$$

$$g(2) = 1 + 4$$

$$g(2) = 5$$



117 $\frac{ax-b}{a-1} = b$ find x

57

$$\frac{ax-b}{a-1} = \frac{b}{1}$$

$$1(ax-b) = b(a-1)$$

$$ax - b = ba - b$$

$$ax - \cancel{b} + \cancel{b} = ba - \cancel{b} + \cancel{b}$$

$$ax = ba$$

$$\frac{ax}{a} = \frac{ba}{a}$$

$$x = b$$

118 $y = mb^2$ find b

$$\frac{y}{m} = \frac{mb^2}{m}$$

$$\frac{y}{m} = b^2$$

$$\pm \sqrt{\frac{y}{m}} = \sqrt{b^2}$$

$$\pm \sqrt{\frac{y}{m}} = b$$

$$b = \sqrt{\frac{y}{m}} \text{ or}$$

$$b = -\sqrt{\frac{y}{m}}$$

(119) $2^{x+1} = 16$ find x

$$2^{x+1} = 2^4$$

$$x+1 = 4$$

$$x+1-1 = 4-1$$

$$x = 3$$

(120) Find the equation of the line with slope $m=3$ thru point $(-3, 6)$.

$$y - y_1 = m(x - x_1)$$

$$y - (6) = 3(x - (-3))$$

$$y - 6 = 3(x + 3)$$

$$y - 6 = 3x + 9$$

$$y - 6 + 6 = 3x + 9 + 6$$

$$y = 3x + 15$$

(60)

(121) Find the equation of the line through the two points $(10, 800)$ and $(12, 900)$. (59)

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

$$y - (800) = \frac{(800) - (900)}{(10) - (12)} (x - (10))$$

$$y - 800 = \frac{800 - 900}{10 - 12} (x - 10)$$

$$y - 800 = \frac{-100}{-2} (x - 10)$$

$$y - 800 = 50(x - 10)$$

$$y - 800 = 50x - 500$$

$$y - 800 + 800 = 50x - 500 + 800$$

$$y = 50x + 300$$

(122) Find the distance between the two points $(5, -2)$ and $(2, 2)$

$$x_1 \ y_1 \quad x_2 \ y_2$$

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

$$d = \sqrt{(5) - (2))^2 + ((-2) - (2))^2}$$

$$d = \sqrt{(5 - 2)^2 + (-2 - 2)^2}$$

$$d = \sqrt{(3)^2 + (-4)^2}$$

$$d = \sqrt{9 + 16}$$

$$d = \sqrt{25}$$

$$d = 5$$

(123) Find the midpoint between the two points $(4, -8)$ and $(-10, 2)$.

(66)

$$\text{midpoint} = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$\text{midpoint} = \left(\frac{(4) + (-10)}{2}, \frac{(-8) + (2)}{2} \right)$$

$$\text{midpoint} = \left(\frac{4 - 10}{2}, \frac{-8 + 2}{2} \right)$$

$$\text{midpoint} = \left(\frac{-6}{2}, \frac{-6}{2} \right)$$

$$\text{midpoint} = (-3, -3)$$

(124) $f(x) = -x^2 + 4x + 5$ find the y-intercept.

find y-intercept let $x=0$

$$f(0) = -(0)^2 + 4(0) + 5$$

$$f(0) = -(0)(0) + 4(0) + 5$$

$$f(0) = 0 + 0 + 5$$

$$f(0) = 5$$

$$(0, 5)$$

(125) $f(x) = -x^2 + 4x + 5$ find the x-intercept
find x-intercept let $y = 0$ (61.)

$$y = f(x) = -x^2 + 4x + 5$$

$$0 = -x^2 + 4x + 5$$

$$-1(0) = -1(-x^2 + 4x + 5) \text{ mult}$$

$$0 = x^2 - 4x - 5$$

$$0 = (x + 1)(x - 5)$$

$$\text{set } x + 1 = 0 \quad \text{OR} \quad x - 5 = 0$$

$$x + 1 - 1 = 0 - 1 \quad \text{OR} \quad x - 5 + 5 = 0 + 5$$

$$x = -1 \quad \text{OR} \quad x = 5$$

(126.) $f(x) = 4x^2 - 8x - 9$ and $g(x) = -2x^2 - 3x + 5$

$$\text{find } (f - g)(x) =$$

$$f(x) - g(x) =$$

$$(4x^2 - 8x - 9) - (-2x^2 - 3x + 5) =$$

$$4x^2 - 8x - 9 + 2x^2 + 3x - 5 =$$

$$6x^2 - 5x - 14 =$$

(127) $f(x) = 2x^2 + 3x + 4$ find $f(x-1)$

(61.)

$$f(x-1) = 2(x-1)^2 + 3(x-1) + 4$$

$$f(x-1) = 2(x-1)(x-1) + 3(x-1) + 4$$

$$f(x-1) = 2(x^2 - 1x - 1x + 1) + 3(x-1) + 4$$

$$f(x-1) = 2(x^2 - 2x + 1) + 3(x-1) + 4$$

$$f(x-1) = 2x^2 - 4x + 2 + 3x - 3 + 4$$

$$f(x-1) = 2x^2 - x + 3$$

(128) $f(x) = x^2 + 6$ find $f(a+h)$

$$f(a+h) = (a+h)^2 + 6$$

$$f(a+h) = (a+h)(a+h) + 6$$

$$f(a+h) = a^2 + ah + ah + h^2 + 6$$

$$f(a+h) = a^2 + 2ah + h^2 + 6$$

(129) $f(x) = x^2 + 8x - 6$ find $\frac{f(x+h) - f(x)}{h}$

$$\frac{((x+h)^2 + 8(x+h) - 6) - (x^2 + 8x - 6)}{h} = \quad (63)$$

$$\frac{(x+h)^2 + 8(x+h) - 6 - x^2 - 8x + 6}{h} =$$

$$\frac{(x+h)(x+h) + 8x + 8h - 6 - x^2 - 8x + 6}{h} =$$

$$\frac{x^2 + xh + xh + h^2 + 8x + 8h - 6 - x^2 - 8x + 6}{h} =$$

$$\frac{xh + xh + h^2 + 8h}{h} =$$

$$\frac{2xh + h^2 + 8h}{h} =$$

$$2x + h + 8 =$$

130. $f(x) = 2x + 3$ and $g(x) = 5x + 8$

find $(f \circ g)(x) =$

$f(g(x)) =$

$f(5x + 8) =$

$2(5x + 8) + 3 =$

$10x + 16 + 3 =$

$10x + 19 =$

131. $f(x) = 2x + 3$ and $g(x) = x^2 + 6x - 5$

find $(g \circ f)(x) =$

$g(f(x)) =$

$g(2x + 3) =$

$(2x + 3)^2 + 6(2x + 3) - 5 =$

$(2x + 3)(2x + 3) + 6(2x + 3) - 5 =$

$4x^2 + 6x + 6x + 9 + 12x + 18 - 5 =$

$4x^2 + 24x + 22 =$

(64)

(132) $f(x) = -1(x-2)^2 + 9$ find the vertex

set $x-2=0$

$x-2+2=0+2$

$x=2$

$f(2) = -1(2-2)^2 + 9$

$f(2) = -1(0)^2 + 9$

$f(2) = -1(0)/0 + 9$

$f(2) = 0 + 9$

$f(2) = 9$

Vertex = $(2, 9)$

(133) $f(x) = -x^2 + 4x + 5$ find vertex use vertex formula

$a = -1, b = 4, c = 5$

$\left(-\frac{b}{2a}, f\left(-\frac{b}{2a}\right)\right)$

$\left(-\frac{b}{2a}, f\left(-\frac{b}{2a}\right)\right) =$

$\left(\frac{-(-4)}{2(-1)}, f\left(\frac{-(-4)}{2(-1)}\right)\right) =$

$\left(\frac{-4}{-2}, f\left(\frac{-4}{-2}\right)\right) =$

$(2, f(2)) =$

$(2, -(2)^2 + 4(2) + 5)$

$(2, -(2)(2) + 4(2) + 5)$

$(2, -4 + 8 + 5)$

$(2, 9)$

134 $f(x) = -250x^2 + 2500x + 50000$ find the vertex
 use vertex formula
 $\left(-\frac{b}{2a}, f\left(-\frac{b}{2a}\right)\right) = \left(-\frac{b}{2a}, f\left(-\frac{b}{2a}\right)\right)$

$\left(\frac{-(2500)}{2(-250)}, f\left(\frac{-(2500)}{2(-250)}\right)\right) =$

$\left(\frac{-2500}{-500}, f\left(\frac{-2500}{-500}\right)\right) =$

$(5, f(5)) =$

$(5, -250(5)^2 + 2500(5) + 50000)$

$(5, -250(5)(5) + 2500(5) + 50000)$

$(5, -6250 + 12500 + 50000)$

$(5, 56250)$

Vertex

135) $f(x) = 4x^2 - 3$ and $g(x) = 5x + 4$

find $(f \cdot g)(x) =$

(6)

$$f(x)g(x) =$$

$$(4x^2 - 3)(5x + 4) =$$

$$20x^3 + 16x^2 - 15x - 12 =$$

136) $f(x) = 3x - 6$ and $g(x) = x^2 - 4$

find $\left(\frac{f}{g}\right)(x) =$

$$a^2 - b^2 = (a+b)(a-b)$$

formula

$$\frac{f(x)}{g(x)} =$$

$$\frac{3x - 6}{x^2 - 4} =$$

$$\frac{3(x - 2)}{(x + 2)(x - 2)} =$$

$$\frac{3}{x + 2} =$$

(137) $\sqrt{180} =$ Prim. 2, 3, 5, 7, ...

$$\sqrt{36 \times 5} =$$

$$\sqrt{36} \sqrt{5} =$$

$$6\sqrt{5} =$$

$$\begin{array}{r} 2 \overline{) 180} \\ 2 \overline{) 90} \\ 3 \overline{) 45} \\ 3 \overline{) 15} \\ 5 \overline{) 5} \\ 1 \end{array}$$

(68)

(138) $\sqrt{169x^6y^1z^9} =$

$$\sqrt{(13)^2 x^6 y^1 z^8 z^1} =$$

$$(13)^1 x^3 z^4 \sqrt{y^1 z^1} =$$

$$13x^3z^4\sqrt{yz} =$$

(139) $\sqrt{3x^3} \sqrt{6x^2} =$

$$\sqrt{3x^3 \cdot 6x^2} =$$

$$\sqrt{18x^5} =$$

$$\sqrt{9 \cdot 2 \cdot x^4 \cdot x^1}$$

$$3x^2\sqrt{2x} =$$

Prim 2, 3, 5, 7.

$$\begin{array}{r} 2 \overline{) 18} \\ 3 \overline{) 9} \\ 3 \overline{) 3} \\ 1 \end{array}$$

(140) $\frac{2}{8-\sqrt{3}}$ rationalize the denominator

(69.)

$$\left(\frac{2}{8-\sqrt{3}}\right)\left(\frac{8+\sqrt{3}}{8+\sqrt{3}}\right) =$$

$$\frac{16+2\sqrt{3}}{64+8\sqrt{3}-8\sqrt{3}-(\sqrt{3})^2} =$$

$$\frac{16+2\sqrt{3}}{64-3} =$$

$$\frac{16+2\sqrt{3}}{61} =$$

$$\frac{16}{61} + \frac{2\sqrt{3}}{61} =$$

$$\frac{16}{61} + \frac{2\sqrt{3}}{61} =$$

$$\frac{16}{61} + \frac{2\sqrt{3}}{61} =$$

(141) $\sqrt{7-x} = x-1$

$$(\sqrt{7-x})^2 = (x-1)^2$$

$$7-x = (x-1)(x-1)$$

$$7-x = x^2 - 1x - 1x + 1$$

$$7-x = x^2 - 2x + 1$$

$$0 = x^2 - 2x + 1 - 7 + x$$

$$0 = x^2 - x - 6$$

$$0 = (x+2)(x-3)$$

$$x+2=0 \text{ OR } x-3=0$$

$$x+2-2=0-2 \text{ OR}$$

$$x=-2$$

$$x-3+3=0+3$$

$$x=3$$

ck

$$\sqrt{7-x} = x-1$$

$$\sqrt{7-(3)} = (3)-1$$

$$\sqrt{4} = 3-1$$

$$2 = 2$$

yes

Good

ck

$$\sqrt{7-x} = x-1$$

$$\sqrt{7-(-2)} = (-2)-1$$

$$\sqrt{7+2} = -2-1$$

$$\sqrt{9} = -3$$

$$3 \neq -3$$

BAD

$$\{3\}$$

(42) $\sqrt[3]{-27a^{11}b^{13}}$ simplifi

(70)

$$\sqrt[3]{(-3)^3 a^9 b^9} =$$

$$(-3)^1 a^3 b^3 \sqrt[3]{a^2 b^1} =$$

$$-3 a^3 b^3 \sqrt[3]{a^2 b} =$$